

COEFFICIENT-MODULATED FIRST-ORDER ALLPASS FILTER AS DISTORTION EFFECT

Jussi Pekonen

TKK Helsinki University of Technology
Department of Signal Processing and Acoustics

DAFx-08 presentation

September 2, 2008



TEKNILLINEN KORKEAKOULU
TEKNISKA HÖGSKOLAN
HELSINKI UNIVERSITY OF TECHNOLOGY
TECHNISCHE UNIVERSITÄT HELSINKI
UNIVERSITÉ DE TECHNOLOGIE D'HELSINKI



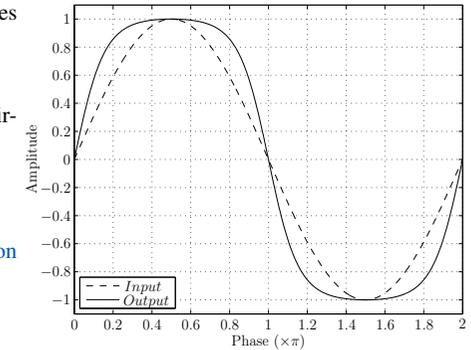
HELSINKI UNIVERSITY OF TECHNOLOGY
Department of Signal Processing and Acoustics

COEFFICIENT-MODULATED FIRST-ORDER ALLPASS FILTER AS
DISTORTION EFFECT
INTRODUCTION

INTRODUCTION

- Distortion is an essential effect especially in electric guitar playing
- Conventionally distortion circuitry modifies the signal amplitude
 - Hyperbolic trigonometric function
 - Nonlinearity often found in electric circuits
 - \sinh (Yeh et al., 2007)
 - \tanh (Huovilainen, 2004)
 - Chebyshev polynomials (Gustafsson et al., 2004)

In figure: $f(x) = \frac{\tanh(2x)}{\tanh(2)}$



Jussi Pekonen

DAFx-08 presentation

September 2, 2008 — Slide 3/11



HELSINKI UNIVERSITY OF TECHNOLOGY
Department of Signal Processing and Acoustics

COEFFICIENT-MODULATED FIRST-ORDER ALLPASS FILTER AS
DISTORTION EFFECT
OUTLINE

OUTLINE

- Introduction
- Coefficient-Modulated First-Order Allpass Filter
- Properties of the Proposed Filter
- Modulation Signal Choice for Electric Guitar Playing
- Conclusions



Source: http://www.ibanez.com/images/artistFeature/_Ihsahn.jpg

Jussi Pekonen

DAFx-08 presentation

September 2, 2008 — Slide 2/11

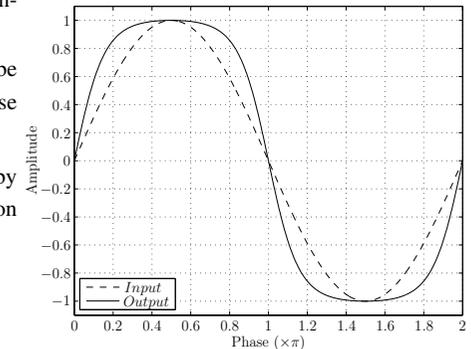


HELSINKI UNIVERSITY OF TECHNOLOGY
Department of Signal Processing and Acoustics

COEFFICIENT-MODULATED FIRST-ORDER ALLPASS FILTER AS
DISTORTION EFFECT
INTRODUCTION

AMPLITUDE DISTORTION BY PHASE MODULATION

- Any signal can be represented at any time instant using amplitude and phase
 - Nonlinear amplitude modification can be interpreted as a modification of the phase increment of the input signal!
- Phase modulation of an arbitrary signal by means of adaptive frequency modulation (AdFM) (Lazzarini et al., 2007)
- Direct AdFM approach not practical
 - Complex control logic
 - Requires a (long) delay line



Jussi Pekonen

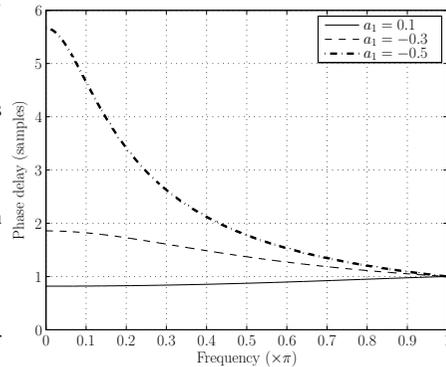
DAFx-08 presentation

September 2, 2008 — Slide 4/11



COEFFICIENT-MODULATED ALLPASS FILTERS

- An allpass filter modifies only the phase of the input signal
 - Frequency-dependent delay
- Allow the coefficients of a low-order allpass filter to be time-varying
 - ⇒ Time-varying frequency-dependent delay
 - Modification of the phase increment of an input signal
 - The resulting filter no longer allpass!



In Figure: Phase delay of a first-order allpass filter $H(z) = \frac{a_1 + z^{-1}}{1 + a_1 z^{-1}}$ for different values of a_1 .



PROPERTIES OF THE PROPOSED FILTER

STABILITY ANALYSIS

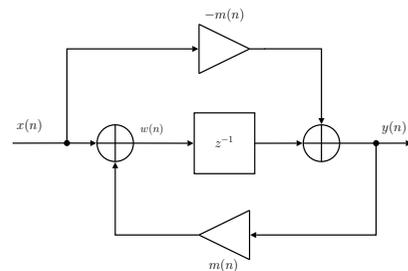
- Stability criteria of time-invariant recursive filters **NOT** applicable to time-varying filters (Laroche, 2007)
- Conditions for stability can be derived from the state-space representation of the filter
 - ⇒ For the proposed filter $|m(n)| \leq 1$

PHASE DELAY AT DC

- $D(n) = \frac{1-m(n)}{1+m(n)}$ (Jaffe and Smith, 1983) ⇒ DC delay always nonnegative
- $m(n) = 1 \Rightarrow D(n) = 0$; $m(n) = -1 \Rightarrow D(n) = \infty$
- When phase delay at DC is large, the filter is highly dispersive
 - ⇒ unnatural artefacts not desirable in distortion effect when the input is a broadband signal



COEFFICIENT-MODULATED FIRST-ORDER ALLPASS FILTER



$$\begin{cases} w(n) = x(n) + m(n)y(n) \\ y(n) = -m(n)x(n) + w(n-1), \end{cases} \text{ and}$$

Expansion of $w(n)$ yields:

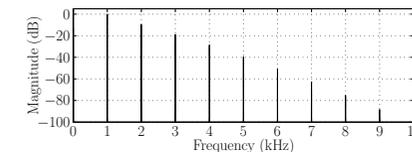
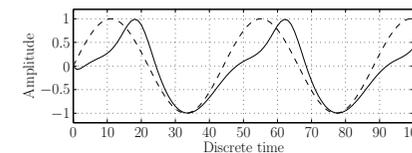
$$y(n) = -m(n)x(n) + (1 - m^2(n-1))x(n-1) + \sum_{k=2}^{\infty} \prod_{l=1}^{k-1} m(n-l)(1 - m^2(n-k))x(n-k).$$

- Time-varying first-order allpass filter used previously in modeling
 - nonlinear spring termination (Pierce and van Duyne, 1997)
 - # Switching between two fixed values
 - tension modulation phenomenon (Pakarinen et al., 2005)
 - # Phase delay at DC limited between zero and one
- Now $m(n)$ is not limited! Except with conditions for stability...

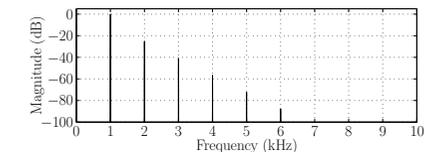
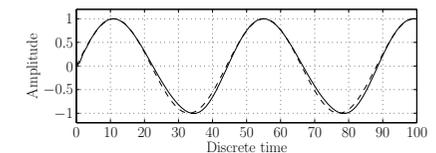


MODULATION SIGNAL CHOICE FOR ELECTRIC GUITAR PLAYING

- For a mild distortion light modulation and for heavier distortion more drastic
- The range of values $m(n)$ gets affects the resulting effect
 - ⇒ Example: input signal a 1000 Hz sine



$$m(n) = 0.45 + 0.45x(n)$$



$$m(n) = -0.45 - 0.45x(n)$$



HOW TO CHOOSE THE MODULATION SIGNAL?

- ↳ The input signal as is
 - ↳ Usually non-smooth ⇒ large distortion
- ↳ Lowpass filtered input signal
- ↳ Constant modulation signal, e.g., a sinusoid

DEMOS

Example 1

I Input signal



II Modulated by lowpass filtered input signal



III Modulated by a 800 Hz sine, (-1, 0.6)



Example 2

I Input signal



II Modulated by lowpass filtered input signal



III Modulated by a 800 Hz sine, (-1, 0.6)



REFERENCES

- F. Gustafsson, P. Connman, O. Oberg, N. Odelholm, and M. Enqvist. System and method for simulation of non-linear audio equipment. U.S. Patent Application 20040258250, 2004.
- A. Huovilainen. Non-linear digital implementation of the Moog ladder filter. In *Proceedings of the 7th International Conference on Digital Audio Effects*, pages 61–64, Naples, Italy, October 2004.
- D. A. Jaffe and J. O. Smith. Extensions of the Karplus-Strong plucked string algorithm. *Computer Music Journal*, 7(2):56–69, Summer 1983.
- J. Laroche. On the stability of time-varying recursive filters. *Journal of the Audio Engineering Society*, 55(6):460–471, June 2007.
- V. Lazzarini, J. Timoney, and T. Lysaght. Adaptive FM synthesis. In *Proceedings of the 10th International Conference on Digital Audio Effects*, pages 21–26, Bordeaux, France, September 2007.
- J. Pakarinen, V. Välimäki, and M. Karjalainen. Physics-based methods for modeling nonlinear vibrating strings. *Acta Acustica united with Acustica*, 91(2):312–325, March/April 2005.
- J. R. Pierce and S. A. van Duyne. A passive nonlinear digital filter design which facilitates physics-based sound synthesis of highly nonlinear musical instruments. *The Journal of the Acoustical Society of America*, 101(2):1120–1126, February 1997.
- D. T. Yeh, J. Abel, and J. O. Smith. Simulation of the diode limiter in guitar distortion circuits by numerical solution of ordinary differential equations. In *Proceedings of the 10th International Conference on Digital Audio Effects*, pages 197–204, Bordeaux, France, September 2007.



CONCLUSIONS

- ↳ Amplitude distortion can be obtained by phase modulation
- ↳ Efficient implementation with a coefficient-modulated low-order allpass filter
- ↳ Coefficient-modulated first-order allpass filter tested
 - ↳ Pros
 - # Computationally efficient
 - # Freedom to choose the modulation signal
 - # Possibility to be almost alias-free
 - ↳ Cons
 - # Only one degree of freedom
 - # Difficulty to choose the modulation signal?
 - # Too simplified approach?

Demos available at: <http://www.acoustics.hut.fi/~jpekonen/Papers/dafx08/>