



# Master's thesis presentation

## Parameter Estimation of a Plucked String Synthesis Model via the Genetic Algorithm

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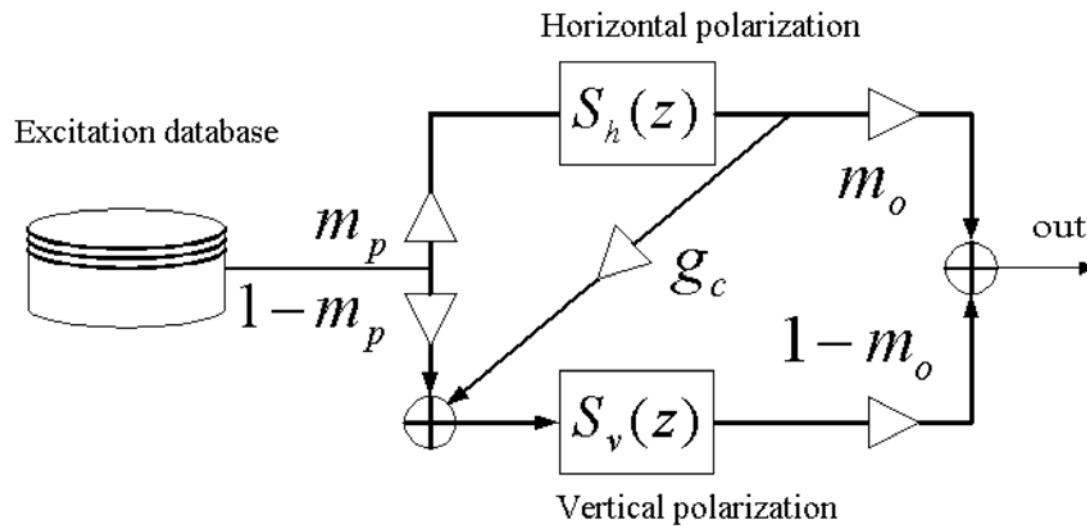
# Outline

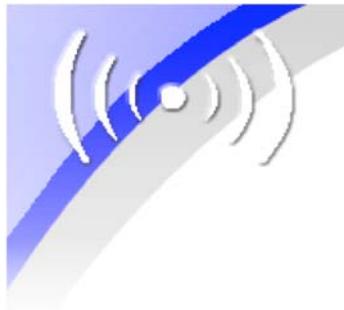
- Plucked string synthesis model
- Estimation procedure
  - Genetic algorithm (GA)
  - Fitness calculation
  - Implementation
- Results
- Conclusions



# Plucked String Synthesis Model

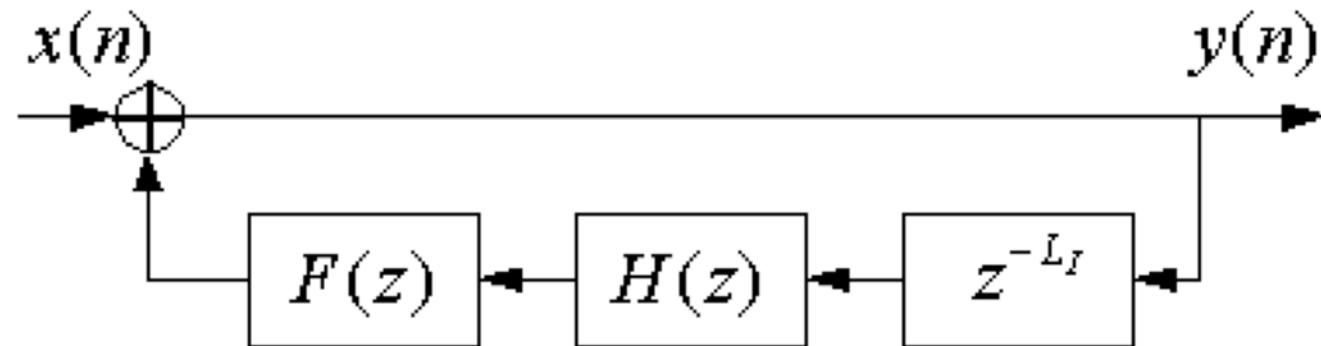
- Proposed by Karjalainen et al. (1998) and based on digital waveguide synthesis theory (Smith, 1992)
- Dual polarization and coupling
- Used intensively to synthesize various plucked string instruments
- Excitation signal is obtained by subtracting the harmonics from recorded tones and equalizing (Välimäki and Tolonen 1998)





## Plucked String Synthesis Model (2)

- Proposed by Jaffe and Smith (1983).
- Delay line and fractional delay filter  $F(z)$  control fundamental frequency
- Filter  $H(z)$  is controlled by loop gain parameter  $g$  and frequency dependent gain  $a$
- Parameters estimation earlier: Algorithm + hand tuning



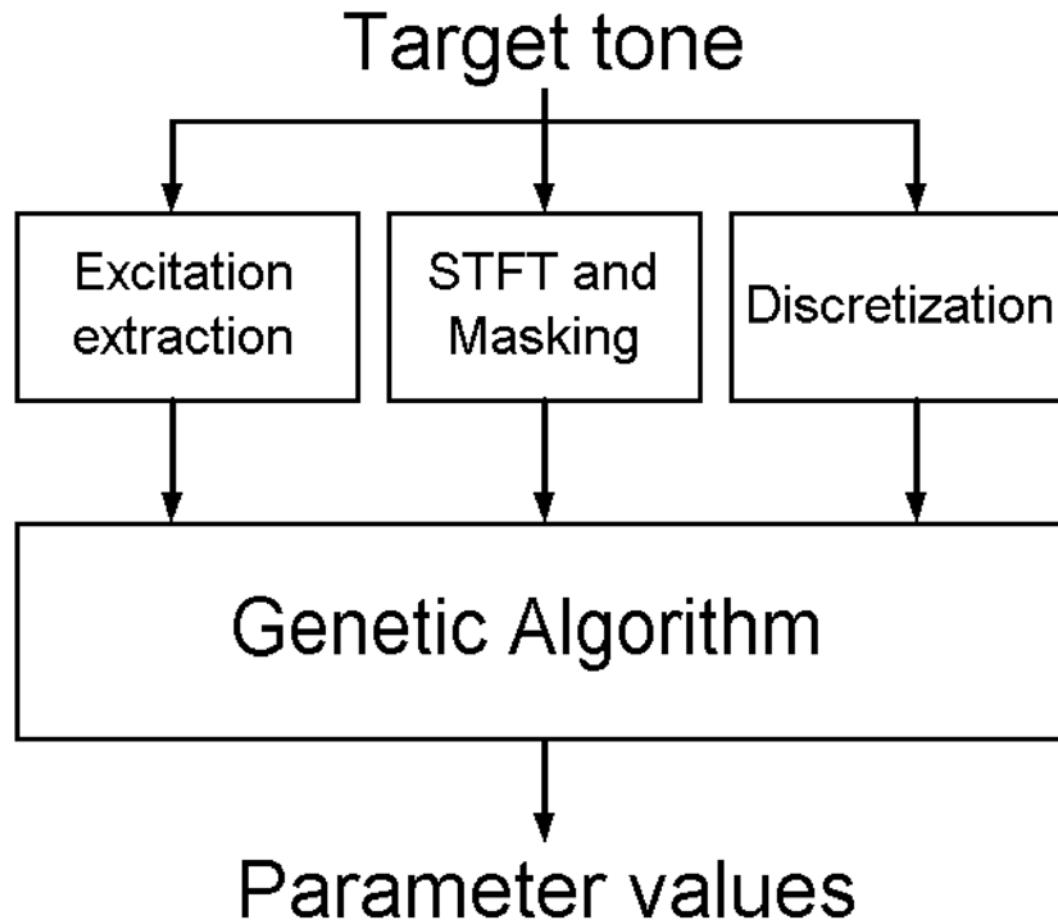


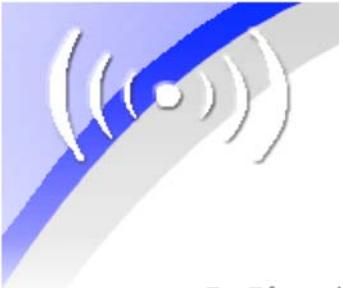
## Parameters to estimate

parameter	control
$f_{0,h}$	fundamental frequency of the horizontal string model
$f_{0,v}$	fundamental frequency of the vertical string model
$g_h$	loop gain of the horizontal string model
$a_h$	frequency dependent gain of the horizontal string model
$g_v$	loop gain of the vertical string model
$a_v$	frequency dependent gain of the vertical string model
$m_p$	input mixing coefficient
$m_o$	output mixing coefficient
$g_c$	coupling gain of the two polarizations



# Parameter Estimation Procedure





## Genetic Algorithm

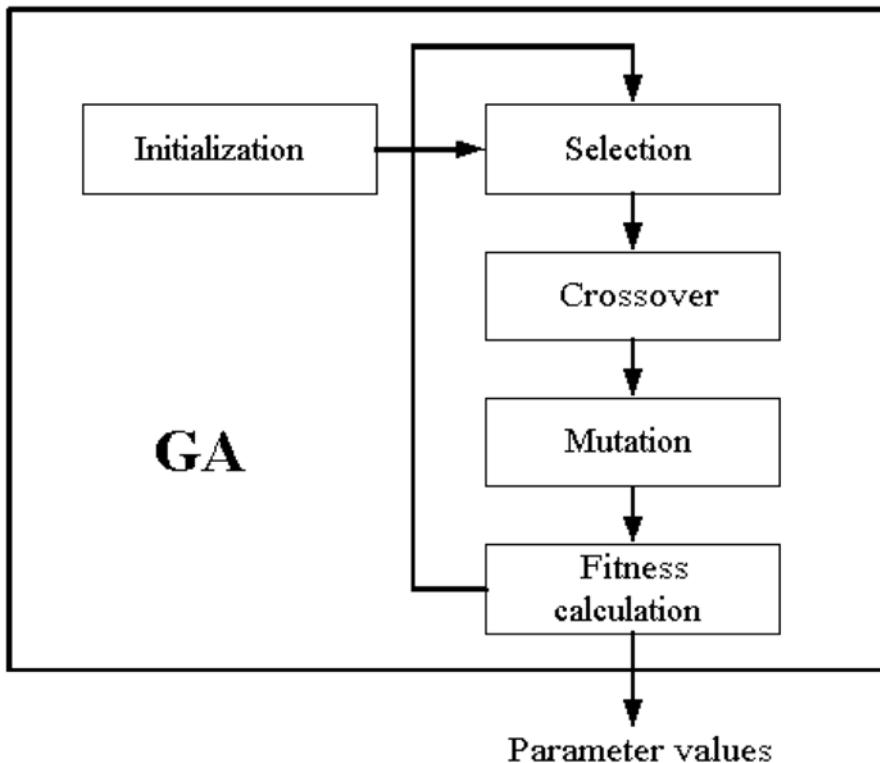
- Mimics the evolution of nature → fittest individuals survive
- Operate on a population of chromosomes

$f_0$	$d_f$	$g_h$	$a_h$	$g_v$	$a_v$	$m_p$	$m_o$	$g_c$
330	0.9	0.991	-0.21	0.922	-0.64	0.11	0.78	0.23

- In every generation, a new set of chromosomes is created by crossing and mutating the fittest individuals
- Desired characteristics are passed into the next generation while imperfect individuals become extinct

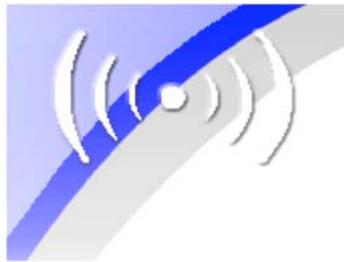


## Genetic Algorithm (2)

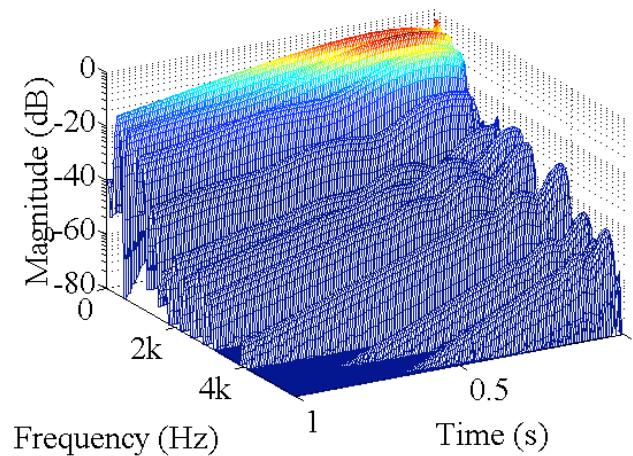
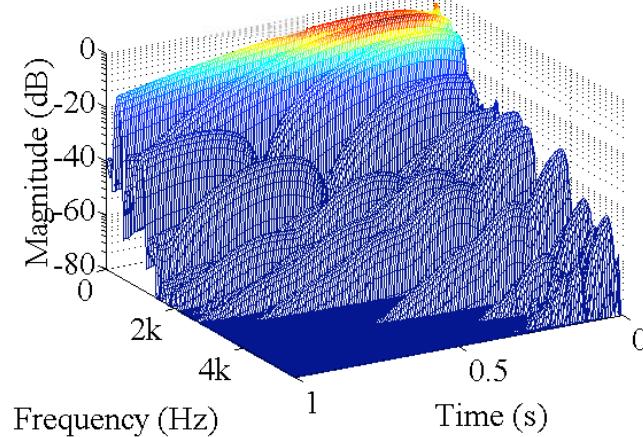


### How to rank sounds?

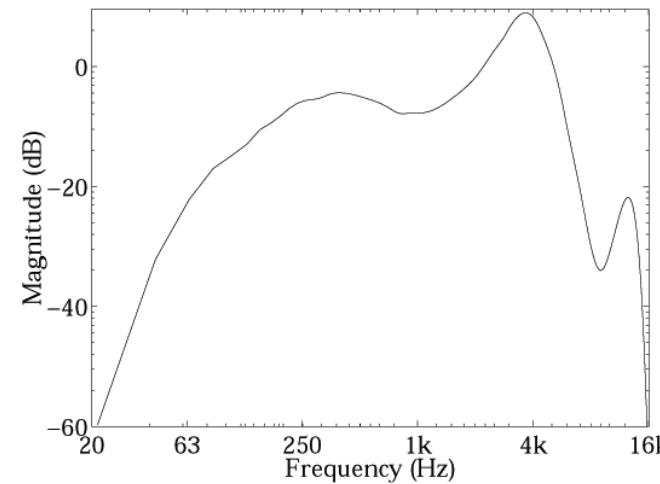
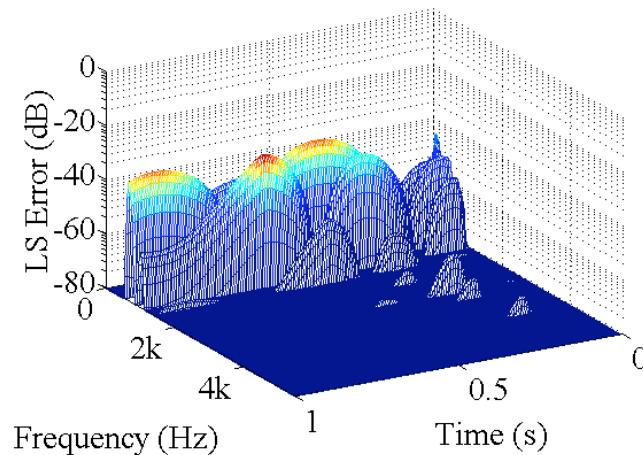
- Listening tests
- Psychoacoustic model
  - Frequency dependence
  - Frequency masking



## Fitness/error calculation



$$(\ )^2 =$$

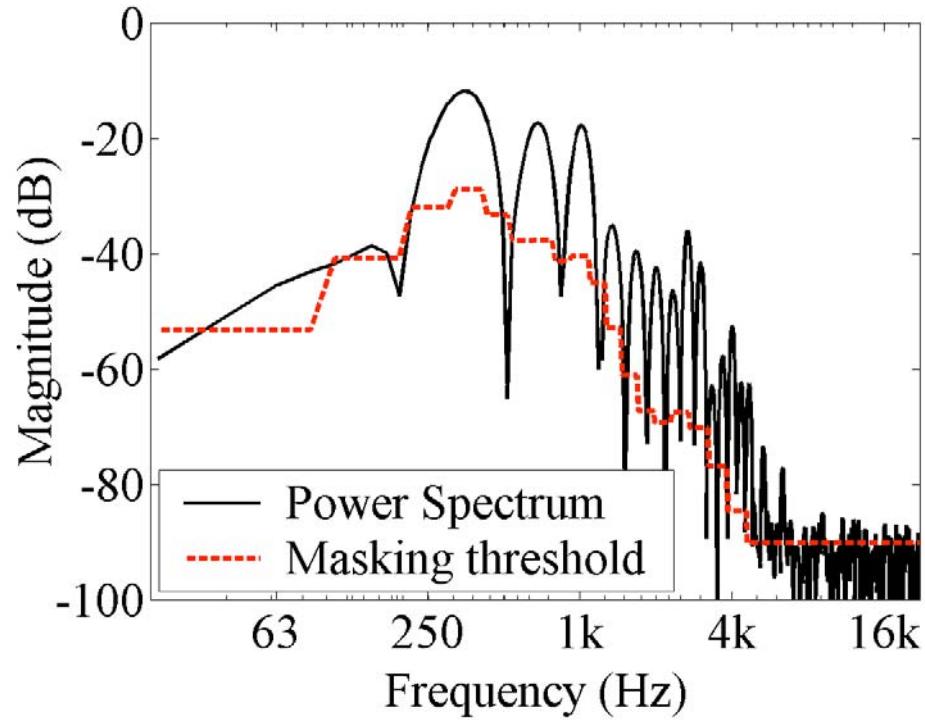


Error =  
21.2



# Calculation of Threshold of Masking

- Based on Johnston's model (Johnston 1988)
  - Energy per critical band
  - Spreading function
  - Final masking threshold
- Frequency components below the threshold are inaudible and therefore unnecessary



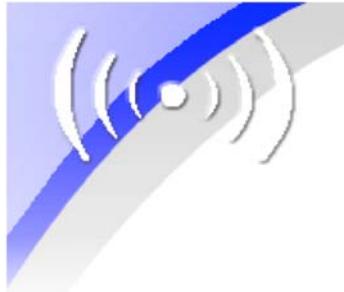


## Discretizing the parameters

- Perceptually reasonable discretion:

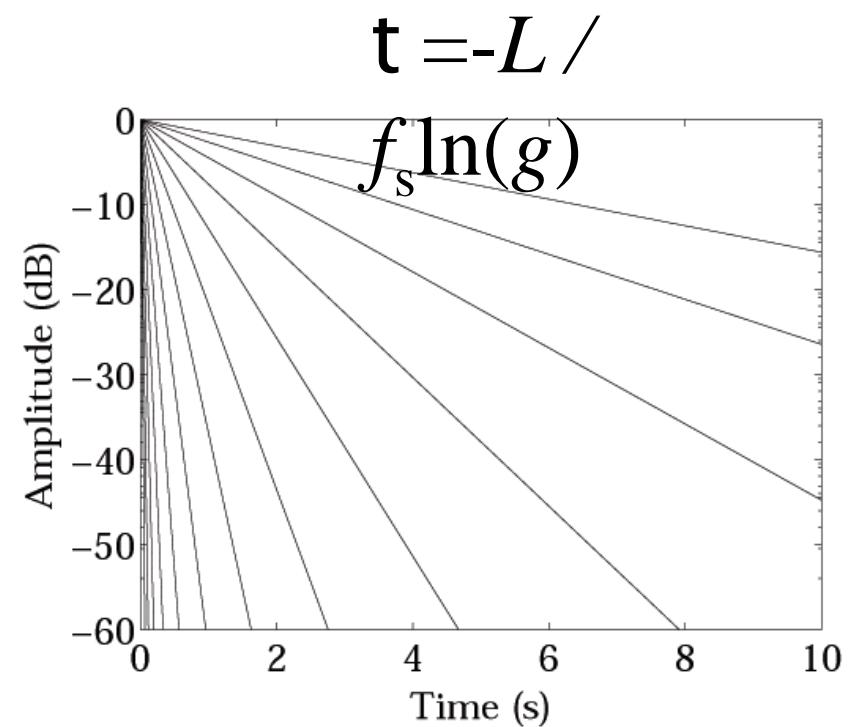
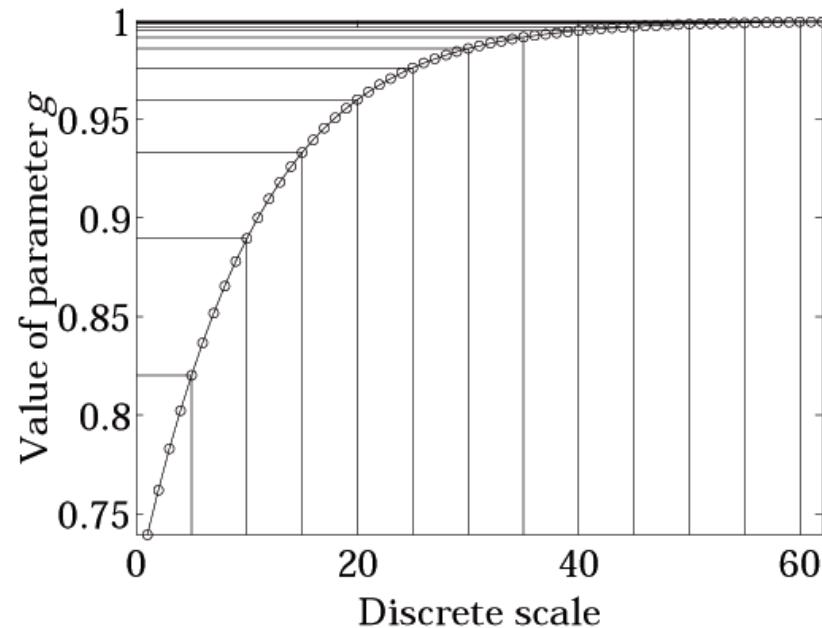
**Use only parameter values that produce different sounding tones!**

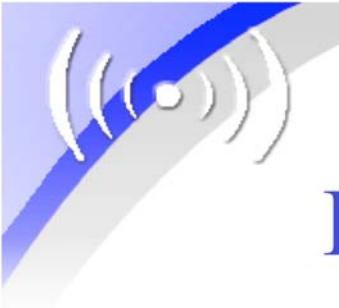
- Based on previous studies, informal listening and sensitivity of the fitness function
- Research is in progress in Aku lab?



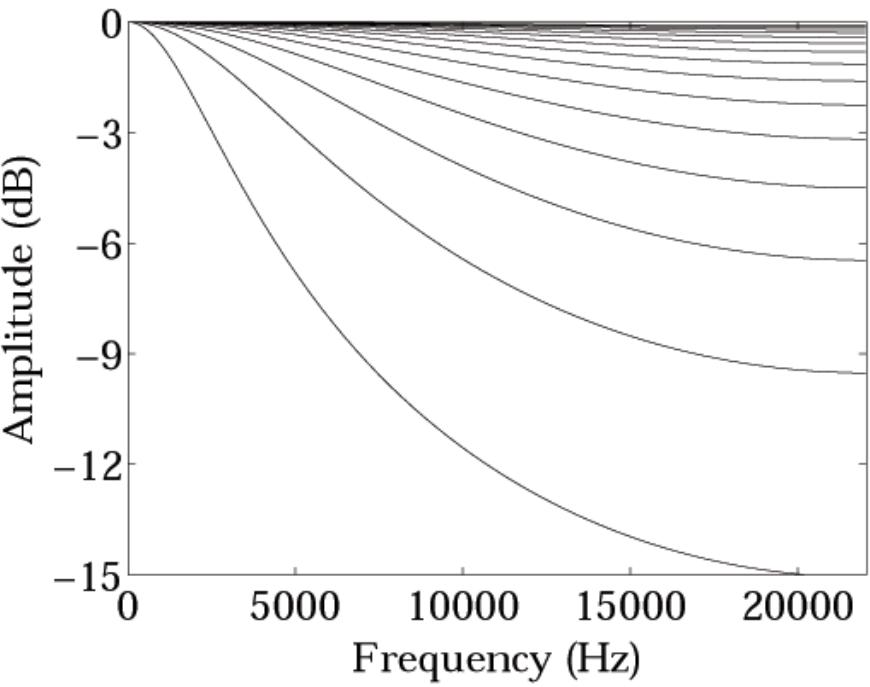
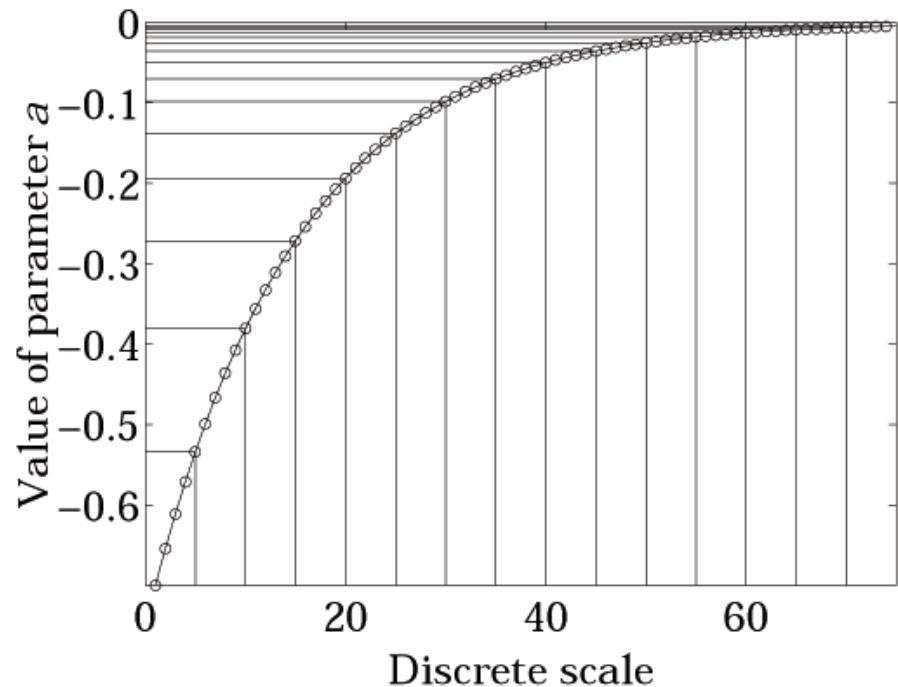
## Discretizing the decay parameters

- Inaudible variation of the time constant  $\tau$  is 75% - 140% and parameter  $a$  between 83% - 116% (Järveläinen and Tolonen 2001)
- We have  $\pm 10\%$  for the  $\tau$  and  $\pm 7\%$  for the  $a$





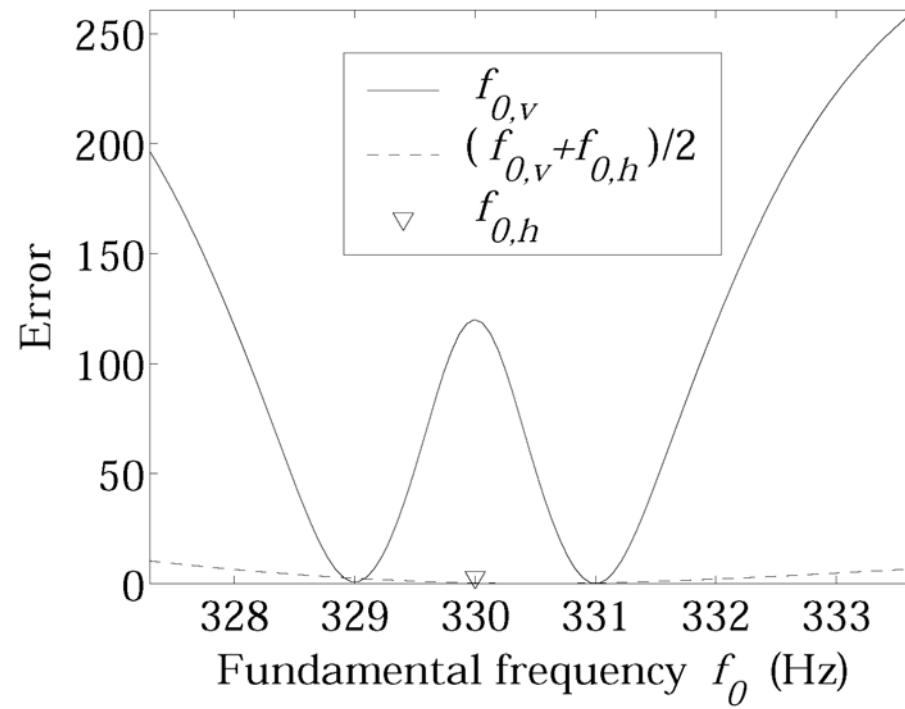
## Discretizing the decay parameters (2)





# Discretizing the fundamental frequency

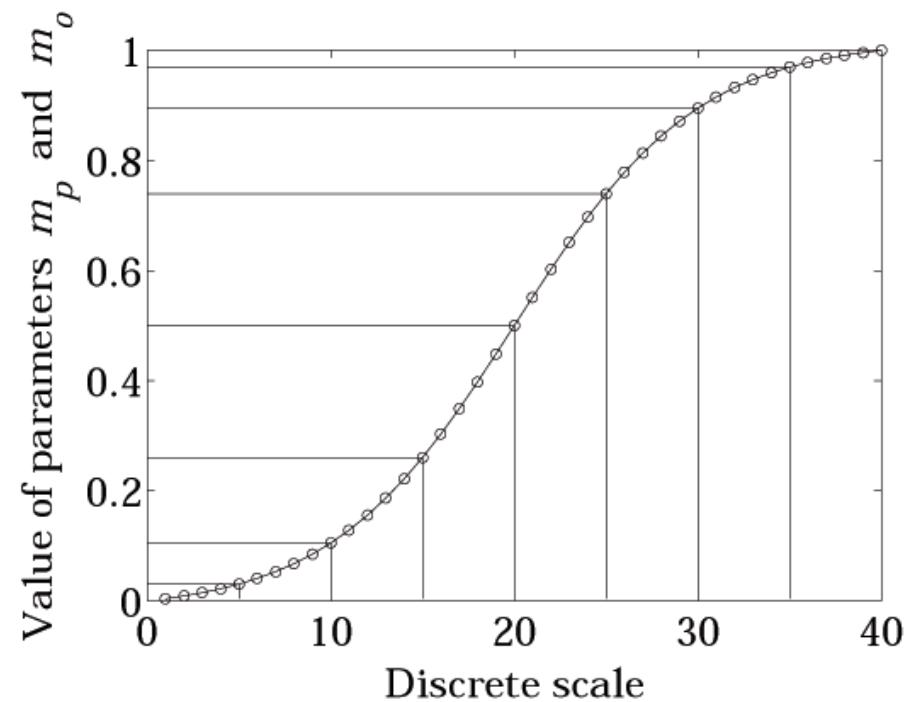
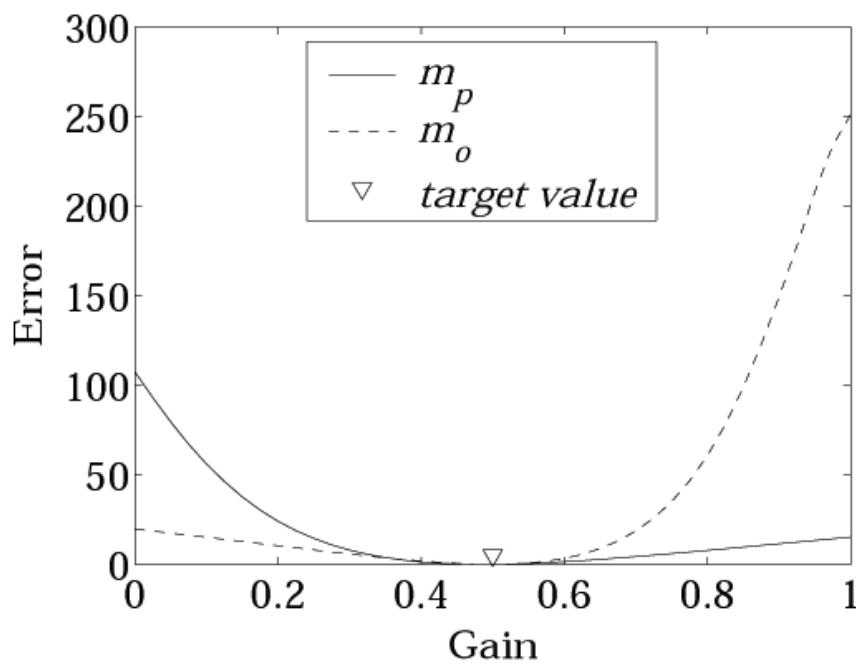
- Sensitivity of the fundamental frequency parameters is examined by varying the parameters and calculating the error
- Beating is significant. Estimate mean frequency  $f_0'$  and difference  $d_f$





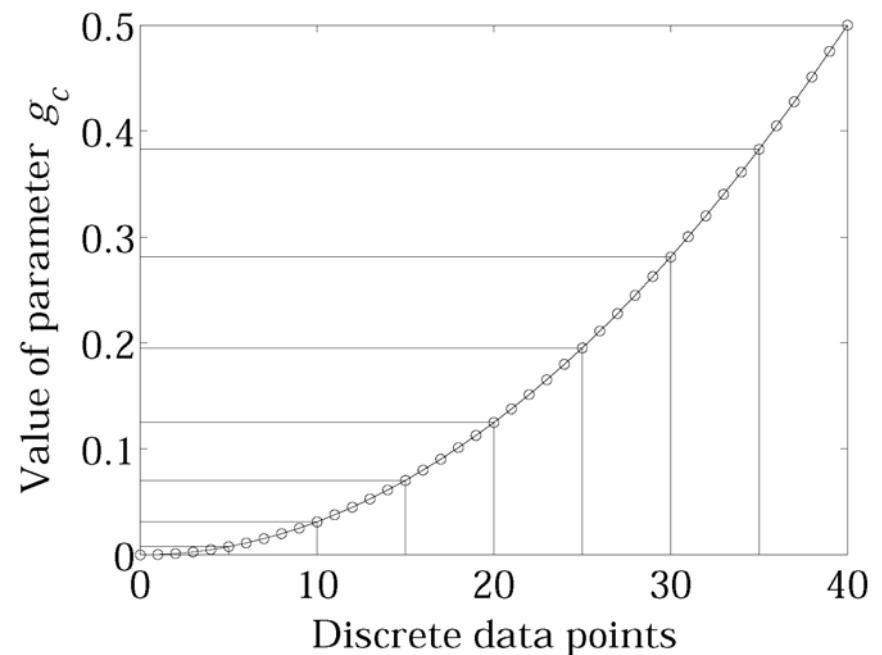
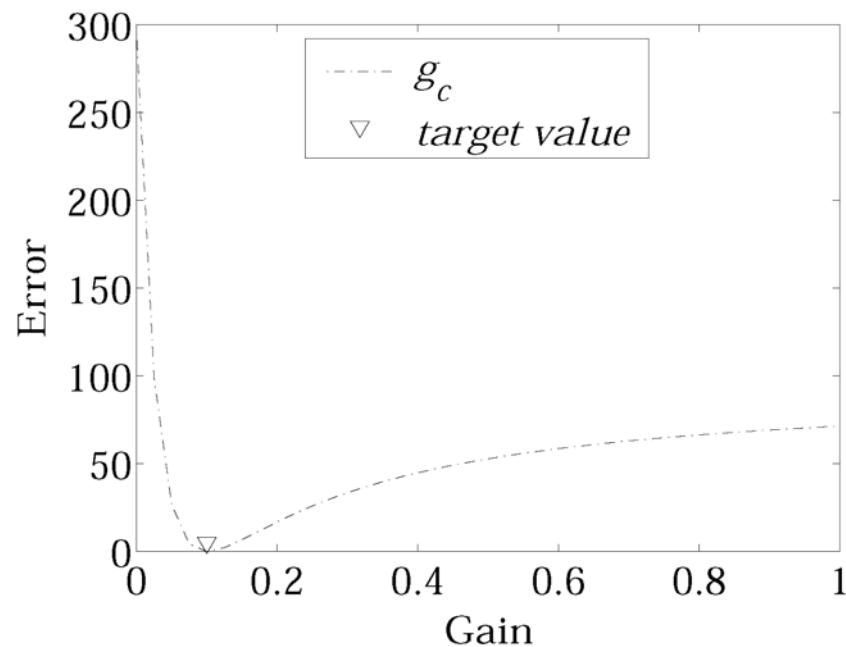
# Discretizing the mixing parameters

- Sensitivity of the mixing parameters is examined by varying the parameters and calculating the error
- Most sensitive at the boundaries which accords with listening





## Discretizing the mixing parameters (2)

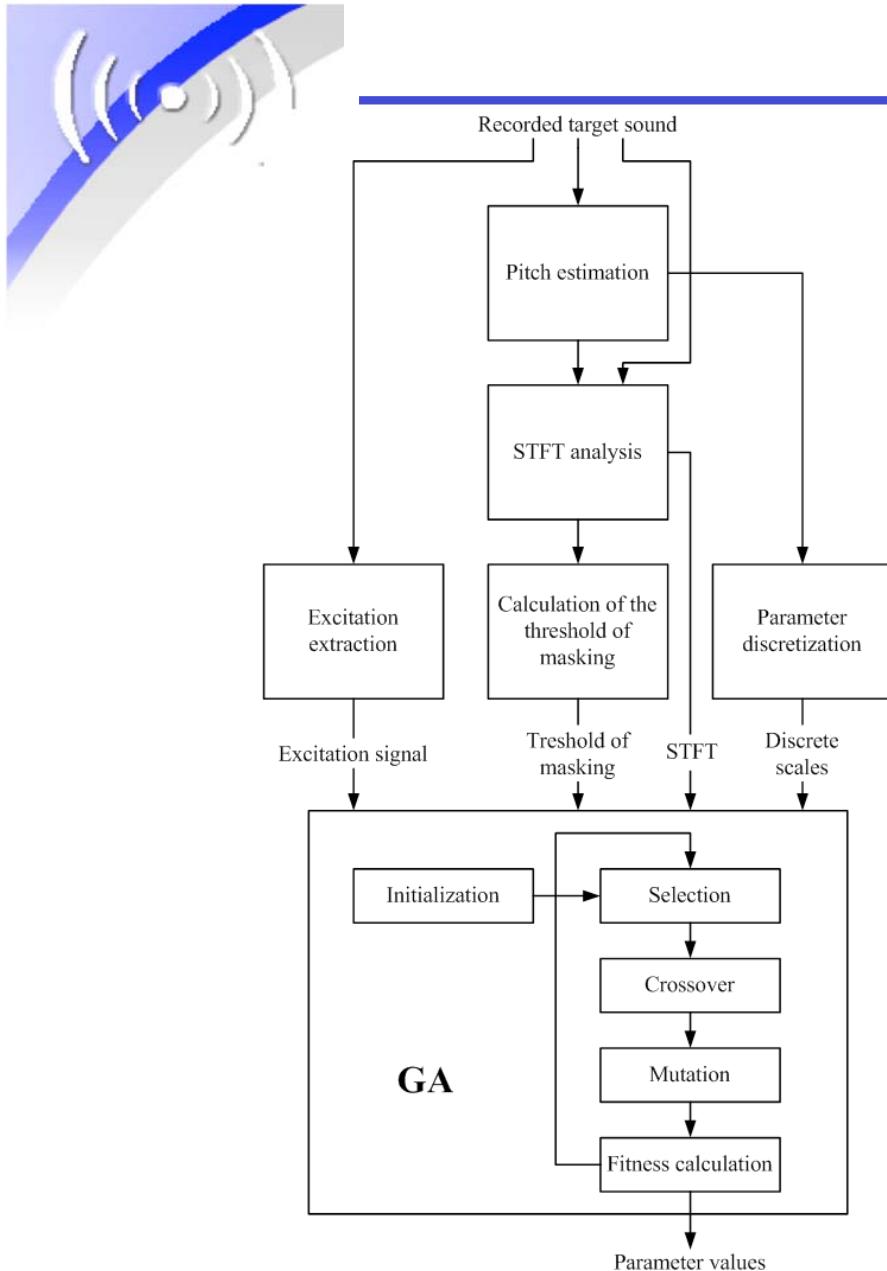




## Discretizing the parameters

- 62 values for  $g$
- 75 values for  $a$
- 20 values for  $f_0'$
- 100 values for  $d_f$
- 40 values for  $m_o$ ,  $m_p$  and  $g_c$
- Total  $2.77 \times 10^{15}$  combinations

# Implementation





## Results

- Procedure was first tested with synthetic tones - target values are known
- Mixing and coupling parameters were noticed not to be orthogonal, implying that similar tones can be synthesized with totally different parameter values
- If  $m_o$  and  $m_p$  are fixed the precise parameter values are estimated when using similar excitation signals



Synthesized  
target tone



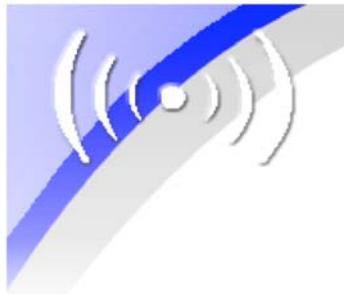
Estimated  
tone with  
error = 0.0112



Estimated  
tone with  
error = 0.464

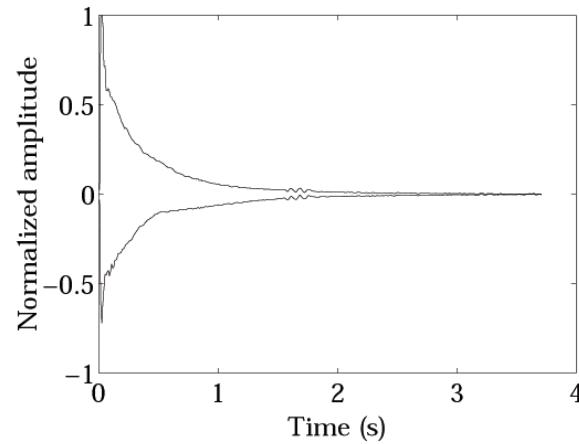


Estimated tone  
with extracted  
excitation signal

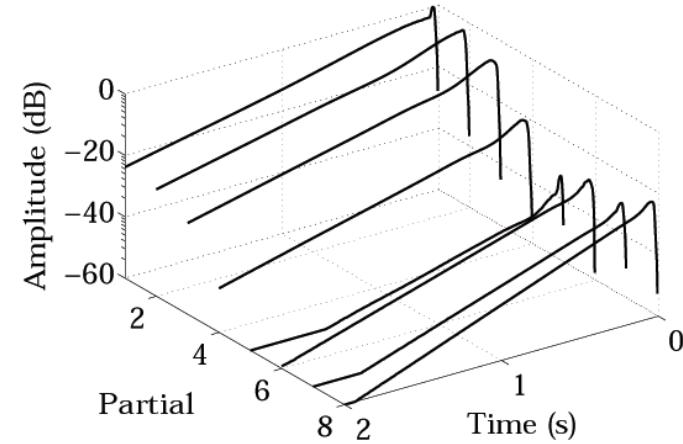
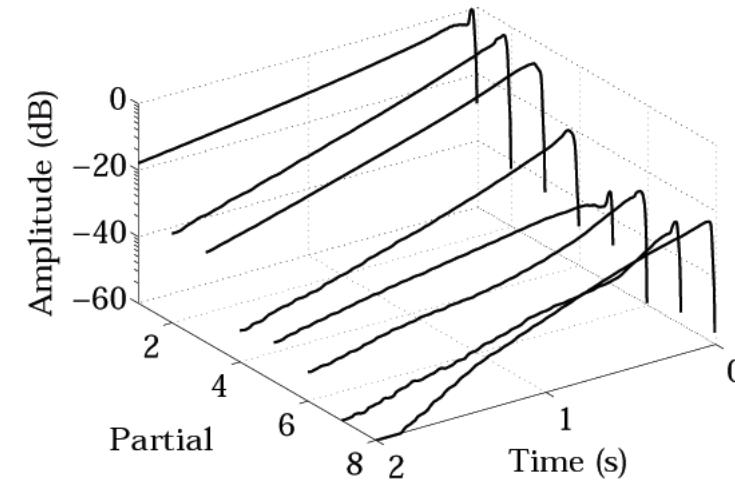
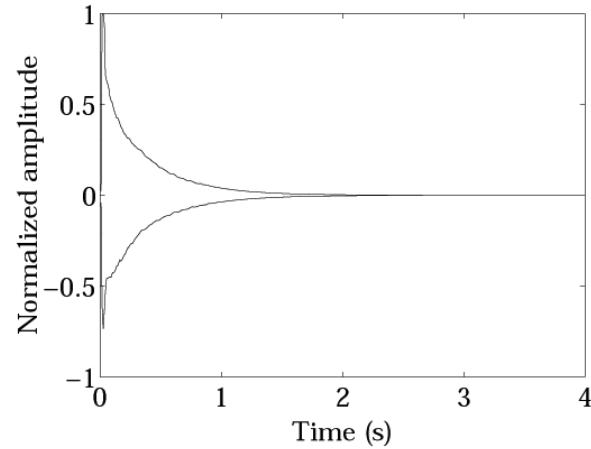


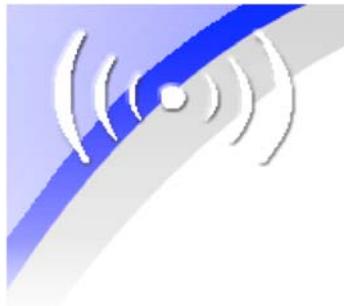
## Results (2)

Real tone



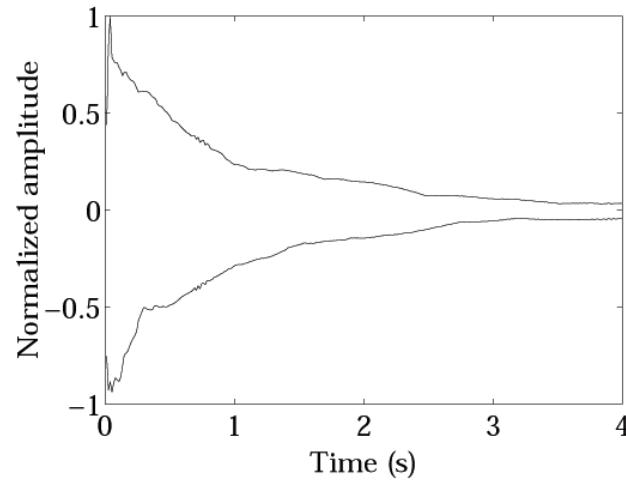
Synthesized tone



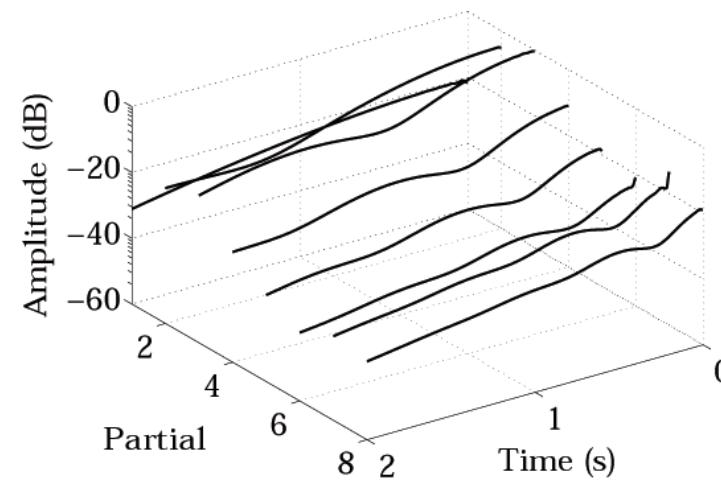
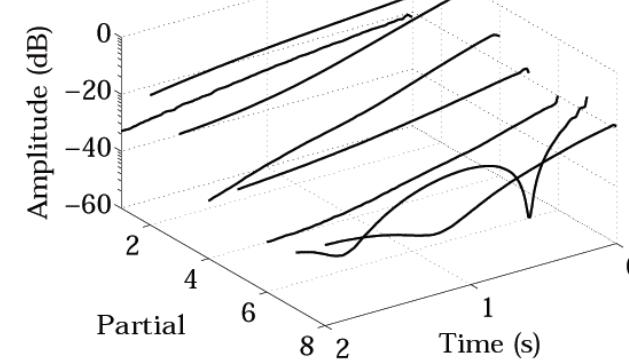
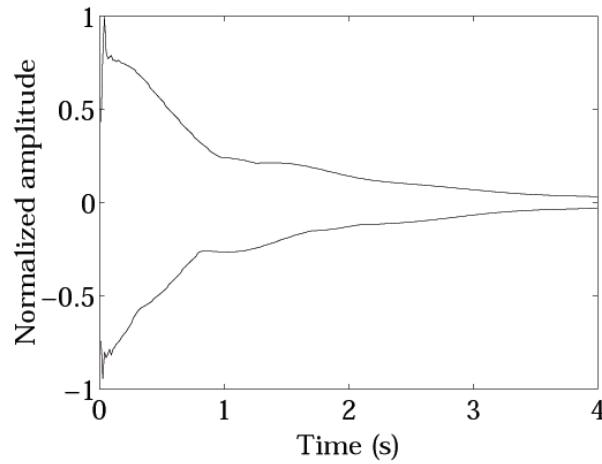


## Results (3)

Real tone



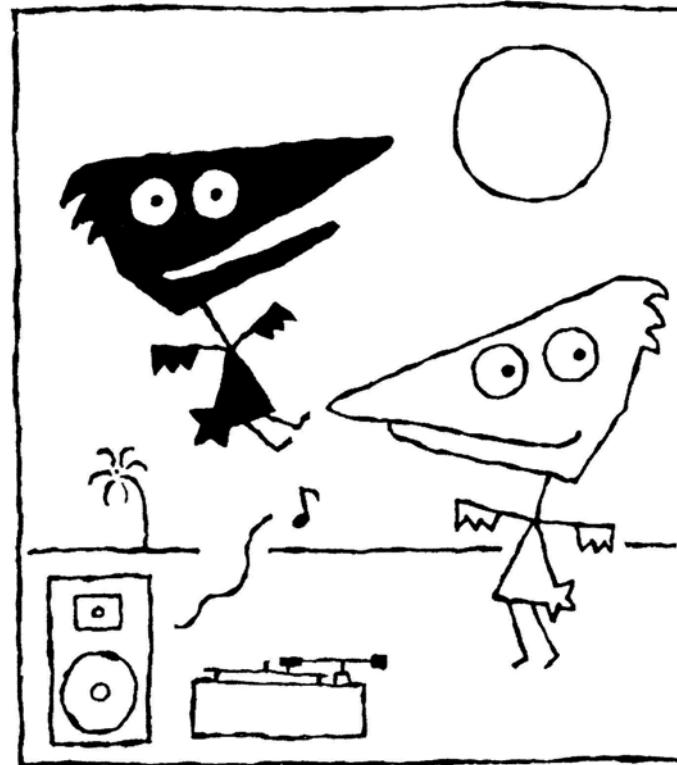
Synthesized tone





## Conclusions

- Genetic algorithm is a universal optimizing tool, which is well suited to our problem
- The most important question is the fitness calculation. How to rank sounds?
- Our procedure works great with “simple” tones
- Our procedure works with “complex” tones, but the result is not identical with the target tone
- Do we want exactly similar tones or just tones that sound realistic?
- Is the expression power of the model enough for “complex” tones?
- $m_o$ ,  $m_p$  and  $g_c$  not orthogonal
- More perceptual studies and better auditory models



<http://acoustics.hut.fi/publications/papers/jasp-ga/>